### Paper / Subject Code: 38911 / Engineering Mathematics-1v

### S.E. SEM IV / COMP / AI & DS / I.T. / CSE / MAY 2024 / 14.05.2024

(Time: 3 hours)

Max. Marks: 80

N.B. (1) Question No. 1 is compulsory.

- (2) Answer any three questions from Q.2 to Q.6. OF EN
- (3) Use of Statistical Tables permitted.
- (4) Figures to the right indicate full marks

Q1. (a) If matrix A = 
$$\begin{bmatrix} -1 & 2 & 3 \\ 0 & 3 & 5 \\ 0 & 0 & -2 \end{bmatrix}$$
 find Eigen values of  $A^3 + 5A + 8I$ . [5]

(b) Evaluate the integral 
$$\int_0^{1+i} (x - y + i x^2) dx$$
 along the parabola  $y^2 = x$ . [5]

(c) Find the z-transform of 
$$f(k) = a^k$$
,  $k \ge 0$ . [5]

(d) Maximise  $z = x_1 + 3x_2 + 3x_3$ 

Subject to 
$$x_1 + 2x_2 + 3x_3 = 4$$

 $2 x_1 + 3x_2 + 5x_3 = 7$  find all basic solutions. Which

of them are basic feasible, And optimal basic feasible solutions.

[5]

Q2 (a) Verify Cayley- Hamilton theorem for the matrix A where 
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & -1 \end{bmatrix}$$

And hence find  $A^{-1}$  and  $A^{-2}$ .

[6]

(b) The means of two random samples of size 9 and 7 are 196.42 and 198.82 respectively

The sum of the squares of the deviations from the means are 26.94 and 18.73 respectively. Can

The samples be considered to have been drawn from same population?

[6]

(c) Solve the L.P.P by using simplex method.

Maximise 
$$z = 3x_1 + 2x_2$$
  
Subject to  $3x_1 + 2x_2 \le 18$ ;  
 $0 \le x_1 \le 4$ ;  
 $0 \le x_2 \le 6$ ;  
 $x_1, x_2 \ge 0$ . [8]

Q3 (a) Find the Laurent's series for

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(b) Using the method of Lagrange's multiplier solve the N.L.P.

Optimise 
$$z = 12 x_1 + 8 x_2 + 6x_3 - x_1^2 - x_2^2 - x_3^2 - 23$$
.  
Subject to  $x_1 + x_2 + x_3 = 10$ .  $x_1, x_2, x_3 \ge 0$ . [6]

(c) Marks obtained by students in an examination follow normal distribution. If 30 %

Of the students got below 35 marks and 10 % got above 60 marks. Find the mean and standard deviation. [8]

- Q4 (a) Find the Eigen values and Eigen vectors of matrix  $A = \begin{bmatrix} 3 & 10 & 5 \\ -2 & -3 & -4 \\ 3 & 5 & 7 \end{bmatrix}$  [6]
- (b) Find inverse z- transform of  $F(z) = \frac{3z^2 18z + 26}{(z-2)(z-3)(z-4)}$  3 < |z| < 4. [6]
- (c) Using the Kuhn Tucker conditions solve the N.L.P.P [8]

Maximise  $z = 12 x_1 x_2 + 2 x_1^2 - 7 x_2^2$ Subject to  $2 x_1 + 5 x_2 \le 98$ ;

$$x_1, x_2 \ge 0.$$

Q5 (a) Show that the matrix  $A = \begin{bmatrix} -9 & 4 & 4 \\ -8 & 3 & 4 \\ -16 & 8 & 7 \end{bmatrix}$  is diagonalisable. Find the diagonal

form D and the Diagonal zing matrix M.

[6]

(b) Find the relative maximum or minimum of the function

$$z = x_1^2 + x_2^2 + x_3^2 - 4x_1 - 8x_2 - 12x_3 + 100.$$
 [6]

(c) Evaluate  $\oint \frac{2z-1}{(2z+1) \ z \ (z+2)}$  dz using Cauchy's residue theorem, where C is the

circle |z|=1. [8]

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- Q6 (a) The number of car accidents in a metropolitan city was found to be 20, 17, 12, 6, 7, 15, 8, 5, 16 and 14 per month respectively. Use  $\chi^2$  test To check whether these frequencies are in agreement with that occurrence was The same during 10 months period. Test at 5 % level of significance.
- (b) Find z transform of  $[2^k \cos(3k+2)]$ ,  $k \ge 0$ . [6]
- (c) Use the dual simplex method to solve the L.P.P.

[8]

Minimise  $z = 2x_1 + x_2$ Subject to  $3x_1 + x_2$ 

Subjectio

$$4 x_1 + 3 x_2 \ge 6;$$

$$x_1 + 2x_2 \le 3$$

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