Paper / Subject Code: 41021 / Engineering Mathematics-IV SE/SEM IV/COMP-IT/NOV 2022/C SCHEME/08.12.2022



Max. Marks: 80

[6]

N.B. (1) Question No. 1 is compulsory.

- (2) Answer any three questions from 0.2 to 0.6.
- (3) Use of Statistical Tables permitted.
- (4) Figures to the right indicate full marks.

Q1 a) If
$$A = \begin{bmatrix} 2 & 4 \\ 0 & 3 \end{bmatrix}$$
 then find the Eigen values of $A^3 + 6A^{-1} + 2I$ [5]

b) Evaluate
$$\int_0^{1+i} (x^2 + iy) dz$$
, along the path (i) $y = x$, (ii) $y = x^2$ [5]

c) Write the dual of the following problem [5]

Maximise
$$z = 3x_1 + 10x_2 + 2x_3$$

subject to
$$2x_1 + 3x_2 + 2x_3 \le 8$$

$$3x_1 - 2x_2 + 4x_3 = 4$$

$$x_1, x_2, x_3 \ge 0$$

d) A certain drug administered to 12 patients resulted in the following change in their Blood Pressure

Can we conclude that drug increase the Blood Pressure?

$$\int_C \frac{1-2z}{z(z-1)(z-2)} dz$$
, Where c is |z|=1.5

(b) Verify Cayley-Hamilton theorem and find A^{-1} for $A = \begin{bmatrix} 1 & 8 \\ 2 & 1 \end{bmatrix}$. Hence, find $2A^3 - A^2 -$ 35A - 44I.

Maximise
$$z = 4x_1 + 10x_2$$

$$Maximise z = 4x_1 + 10x_2$$

$$2x_1 + x_2 \le 50$$
$$2x_1 + 5x_2 \le 100$$

$$2x_1 + 3x_2 \le 90$$

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Subject to

Q3 a) Based on the following data determine if there is a relation between literacy and smoking

	C1	Non amakara	[6]
	Smokers	Non-smokers	[6]
Literates	83	57	
Illiterates	45	68	

(Given that Critical value of chi-square 1 d. f and 5% L.O.S is 3.841

b) Obtain Laurent's series expansion of
$$f(z) = \frac{1}{z^2 + 4z + 3}$$
 [6]

when (i)
$$|z| < 1$$
 (ii) $1 < |z| < 3$ (ii) $|z| > 3$

Optimise
$$z = x_1^2 + x_2^2 + x_3^2$$

Subject to $x_1 + x_2 + 3x_3 = 2$
 $5x_1 + 2x_2 + x_3 = 5$
 $x_1, x_2, x_3 \ge 0$

Q4a) Using the method of Lagrange's multipliers solve the following N.L.P.P [6]

Optimise
$$z = x_1^2 + x_2^2 + x_3^2 - 10x_1 - 6x_2 - 4x_3$$

Subject to $x_1 + x_2 + x_3 = 7$

$$x_1, x_2, x_3 \ge 0$$

b) Find the inverse Z-transform of
$$\frac{1}{z^2-3z+2}$$
, if ROC is (i) $|z| < 1$ (ii) $|z| > 2$ [6]

c) Show that the matrix
$$A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$
 is diagonalizable. Find the transforming matrix and the diagonal matrix.

Q5a) Find
$$Z\{f(k) * g(k)\}$$
 if $f(k) = \left(\frac{1}{2}\right)^k$, $g(k) = \cos \pi k$ [6]

$$A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -5 & -2 \end{bmatrix}$$

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c) Solve by the dual Simplex Method

[8]

Minimise
$$z = x_1 + x_2$$

Subject to
$$2x_1 + x_2 \ge 2$$

$$-x_1 - x_2 \ge 1$$

$$x_1, x_2 \ge 0$$

Q6a) Find
$$Z\{2^k \cos(3k+2)\}, k \ge 0$$
.

[6]

- b) If the heights of 500 students is normally distributed with mean 68 inches and standard deviation 4 inches, estimate the number of students having heights (i) greater than 72 inches
- (ii) less than 62 inches (iii) between 65 and 71 inches

[6]

c) Using Kuhn Tucker conditions, solve the following NLPP

[8]

Maximise

$$z = 2x_1^2 - 7x_2^2 + 12x_1x_2$$

$$2x_1 + 5x_2 \le 98$$

$$x_1,x_2\geq 0$$

students having h

inches

following VI PP

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